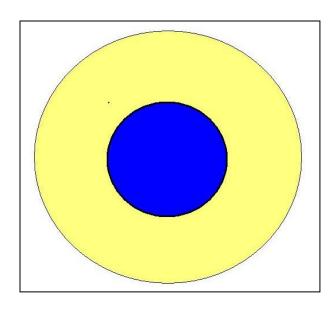
How to Build a Planet from the Inside Out!



The planet Osiris orbits 7 million kilometers from the star HD209458 located 150 light years away in the constellation Pegasus. The Spitzer Space Telescope has recently detected water, methane and carbon dioxide in the atmosphere of this planet. The planet has a mass that is 69% that of Jupiter, and a volume that is 146% greater than that of Jupiter.

By knowing the mass, radius and density of a planet, astronomers can create plausible models of the composition of the planet's interior. Here's how they do it!

Among the first types of planets being detected in orbit around other stars are enormous Jupiter-sized planets, but as our technology improves, astronomers will be discovering more 'super-Earth' planets that are many times larger than Earth, but not nearly as enormous as Jupiter. To determine whether these new worlds are Earth-like, they will be intensely investigated to determine the kinds of compounds in their atmospheres, and their interior structure. Are these super-Earths merely small gas giants like Jupiter, icy worlds like Uranus and Neptune, or are they more similar to rocky planets like Venus, Earth and Mars?

Problem 1 - A hypothetical planet is modeled as a sphere. The interior has a dense rocky core, and on top of this core is a mantle consisting of a thick layer of ice. If the core volume is 4.18×10^{12} cubic kilometers and the shell volume is 2.92×10^{13} cubic kilometers, what is the radius of this planet in kilometers?

Problem 2 - If the volume of Earth is 1.1×10^{12} cubic kilometers, to the nearest whole number, A) how many Earths could fit inside the core of this hypothetical planet? B) How many Earths could fit inside the mantle of this hypothetical planet?

Problem 3 - Suppose the astronomer who discovered this super-Earth was able to determine that the mass of this new planet is 8.3 times the mass of Earth. The mass of Earth is 6.0×10^{24} kilograms. What is A) the mass of this planet in kilograms? B) The average density of the planet in kilograms/cubic meter?

Problem 4 - Due to the planet's distance from its star, the astronomer proposes that the outer layer of the planet is a thick shell of solid ice with a density of 1000 kilograms/cubic meter. What is the average density of the core of the planet?

Problem 5 - The densities of some common ingredients for planets are as follows:

Granite 3,000 kg/m³; Basalt 5,000 kg/m³; Iron 9,000 kg/m³

From your answer to Problem 4, what is the likely composition of the core of this planet?

Problem 1 - The planet is a sphere whose total volume is given by V = $4/3 \pi R^3$. The total volume is found by adding the volumes of the core and shell to get V = $4.18 \times 10^{12} + 2.92 \times 10^{13} = 3.34 \times 10^{13}$ cubic kilometers. Then solving the equation for R we get R = $(3.34 \times 10^{13} / (1.33*3.14))^{1/3} = 19,978$ kilometers. Since the data is only provided to 3 place accuracy, the final answer can only have three significant figures, and with rounding this equals a radius of R = 20,000 kilometers.

Problem 2 - If the volume of Earth is 1.1×10^{12} cubic kilometers, to the nearest whole number, A) how many Earths could fit inside the core of this hypothetical planet? Answer: $V = 4.18 \times 10^{12}$ cubic kilometers $/ 1.1 \times 10^{12}$ cubic kilometers = 4 Earths.

B) How many Earths could fit inside the mantle of this hypothetical planet? Answer: $V = 2.92 \times 10^{13}$ cubic kilometers / 1.1 x 10¹² cubic kilometers = 27 Earths.

Problem 3 - What is A) the mass of this planet in kilograms? Answer: $8.3 \times 6.0 \times 10^{24}$ kilograms = 5.0×10^{25} kilograms.

B) The average density of the planet in kilograms/cubic meter?

Answer: Density = total mass/ total volume

= 5.0×10^{25} kilograms/3.34 x 10^{13} cubic kilometers

= 1.5 x 10¹² kilograms/cubic kilometers.

Since 1 cubic kilometer = 10^9 cubic meters,

= 1.5 x 10¹² kilograms/cubic kilometers x (1 cubic km/10⁹ cubic meters)

= 1,500 kilograms/cubic meter.

Problem 4 - We have to subtract the total mass of the ice shell from the mass of the planet to get the mass of the core, then divide this by the volume of the core to get its density. Mass = Density x Volume, so the shell mass is 1,000 kg/ m³ x 2.92 x 10^{13} km³ x $(10^9$ m³/km³) = 2.9 x 10^{25} kg. Then the core mass = 5.0×10^{25} kilograms - 2.9×10^{25} kg = 2.1×10^{25} kg. The core volume is 4.18×10^{12} km³ x $(10^9$ m³/km³) = 4.2×10^{21} m³, so the density is $D = 2.1 \times 10^{25}$ kg / 4.2×10^{21} m³ = 5,000 kg/ m³.

Problem 5 - The densities of some common ingredients for planets are as follows:

Granite 3,000 kg/m³; Basalt 5,000 kg/m³; Iron 9,000 kg/m³

From your answer to Problem 4, what is the likely composition of the core of this planet? Answer: Basalt.

Note that, although the average density of the planet (1,500 kg/m³) is not much more than solid ice (1,000 kg/m³), the planet has a sizable rocky core of higher density material. Once astronomers determine the size and mass of a planet, these kinds of 'shell-core' models can give valuable insight to the composition of the interiors of planets that cannot even be directly imaged and resolved! In more sophisticated models, the interior chemistry is linked to the temperature and location of the planet around its star, and proper account is made for the changes in density inside a planet due to compression and heating. The surface temperature, which can be measured from Earth by measuring the infrared 'heat' from the planet, also tells which compounds such as water can be in liquid form.